

# Theoretical analysis and experiment on Eu reduction in alumina optical materials

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**Abstract:** Density functional theory simulation with a U correction (DFT + U) was adopted to predict the proper experimental conditions required to generate divalent europium ( $\text{Eu}^{2+}$ ) in  $\alpha\text{-Al}_2\text{O}_3$  host material consolidated via vacuum consolidation. Accordingly, samples of 0.1 at%  $\text{Eu}^{2+}:\alpha\text{-Al}_2\text{O}_3$  were obtained by gelcasting, followed by high vacuum sintering process ( $<10^{-3}$  Pa). The room temperature photoluminescence excitation and emission spectra of this composition were examined and characteristic broad band positioned in the blue part of spectrum was detected under UV excitation. This luminescence decay trace had two-exponential character and the average decay time of 0.1 at%  $\text{Eu}^{2+}:\alpha\text{-Al}_2\text{O}_3$  was 0.080ms.

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**OCIS codes:** (160.2540) Fluorescent and luminescent materials; (160.1890) Detector materials; (160.2220) Defect-center materials; (160.4670) Optical materials.

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## 1. Introduction

Optical materials based on rare earth activation center, such as neodymium and europium ions, are critical for a wide range of applications including phosphors [1–3], lasers [4], and scintillator materials [5, 6] for ionizing radiation detection [7]. Their optical properties are very sensitive to the host lattice, i.e., crystal field strength, covalency, cation size, etc., and

therefore considerable attention has been paid to the search for host materials with high performance and reliability. Many of the recently developed hosts are halides [6, 8–14]. They provide high light output and reasonable scintillation decay time, but suffer from sensitivity to moisture and low mechanical strength, which has substantially limited their applications, especially as scintillators. Oxide ceramics, on the other hand, possess high chemical stability and high transparency, and thus can be ideal candidates for the next generation of scintillator materials. For example, it was recently reported that Eu-doped garnet ( $\text{Y}_3\text{Al}_5\text{O}_{12}$ ) scintillators show very promising scintillation properties [15]. The widely available  $\alpha\text{-Al}_2\text{O}_3$  has also been considered for cryogenic phonon detector designated for the Dark Matter experiment [16, 17]. Indeed, these materials can also provide good mechanical properties, excellent refractory character, high chemical stability and optical transmission over a wide range of wavelengths.

However, efficient identification of high-performance host oxide with proper fabrication conditions is challenging. The chemical state of many rare earth activation centers (i.e., valence) is sensitive to the synthesis condition, and this is coupled with the stringent sintering conditions required to achieve transparency in polycrystalline oxide materials. Predictive method based on computations are also lacking, due to the difficulty in accurately capture the electronic behavior, particularly for the f-electrons, in different atomic environments, at realistically low doping concentration (tenths of a percent), and as a function of experimental conditions. It is therefore no surprise that determining the correct experimental conditions so far has been largely relying on trial and error. In this paper, we present a protocol to use *ab-initio* simulations based on density functional theory (DFT) to guide the experimental synthesis of rare earth doped transparent polycrystalline ceramics. Using  $\text{Eu}^{2+}$  doped  $\alpha\text{-Al}_2\text{O}_3$  as an example, we present the evidence that sophisticated DFT simulations can provide critical guidance for assessing experimental feasibility and selecting effective synthesis conditions. This provides the basis for efficient predictive tools based on computations that would enable high-throughput screening of the similar materials. For validation,  $\text{Eu}:\text{Al}_2\text{O}_3$  ceramics were synthesized by gelcasting techniques and vacuum sintering method with photoluminescence properties and decay time characterized here.

## 2. Method

### 2.1 Density functional theory simulations with *U* correction (DFT + *U*)

The *ab initio* simulations were performed with VASP, a plane wave DFT package [18]. PBE exchange and correlation functional was used with the plane wave cutoff set to 500 eV. To properly describe the f-electrons of Eu ions, we applied the DFT + *U* method with an effective *U* value of 6 eV, according to several previous simulation studies of Eu-containing compounds [19–21]. We paid particular attention to the issues of unphysical sub-orbital occupations raised in recent DFT + *U* studies, which can lead to incorrect energetics and ionic structures in some materials [22–25]. With a simple scheme proposed recently, which involves ramping the *U* value iteratively during ionic relaxation [24, 25], we did not find sub-orbital occupations significantly more stable than the ones obtained by the standard method for the systems studied here, although more thorough investigation might be needed.

The target doping concentration of synthesized  $\text{Eu}:\text{Al}_2\text{O}_3$  is 0.1 at. % is well below the dilute solution limit. For example, the probability of a Eu substitution have no other Eu substitution in a nearest neighbor configuration, i.e., all three nearest cation sites around the Eu are occupied by Al ions, is  $(99.9\%)^3 = 99.7\%$  in a random distribution. Similarly, in the case of  $\text{Eu}^{2+}$  compensated with oxygen vacancy, the probability of a Eu dopant in the  $\alpha\text{-Al}_2\text{O}_3$  lattice (assuming six coordinated, see detailed discussions below) does not have neighboring oxygen vacancy is 99.8%. Therefore, it is necessary to consider the defects as isolated. We note, however, our simulations indeed found considerable association between certain defects, especially in the case of  $\text{Eu}^{2+}$  and oxygen vacancy (binding energy of 2.5 eV in a  $3 \times 3 \times 1$  supercell). Such association would inevitably begin to manifest when the doping concentration increases, and should be taken into consideration in heavily doped cases.

Within the plane wave DFT frame, the periodic system containing isolated defects must be dealt with care. Especially, charged defects, which are neutralized with electron jellium in the present study, can considerably slow the convergence against system size [26]. To resolve this issue, we adopted a correction scheme proposed by Hine *et al* [27]. In this scheme, a series of supercells of different sizes and shapes containing the same defect are simulated, and the corrected energy is obtained by extrapolating a linear relationship between the energy and the Madelung potential of each supercell (calculated as a function of the defect charge and cell geometry) to infinite system size. For each charged defect in the present study, we fully relaxed four hexagonal corundum supercells ( $2 \times 2 \times 1$ ,  $2 \times 2 \times 2$ ,  $3 \times 3 \times 1$ ,  $2 \times 2 \times 3$ ) to extrapolate the corrected defect energy. For  $\text{Eu}^{3+}$  substitution, no addition charge is involved and the results from  $3 \times 3 \times 1$  supercell (270 atoms) are used. For all the structures, relaxation was conducted until forces on all the atoms are below 0.01 eV/Å.

## 2.2 Synthesis and characterization of Eu: $\text{Al}_2\text{O}_3$

0.1 at. % Eu:  $\text{Al}_2\text{O}_3$  were synthesized by gelcasting technique. Vacuum sintering method were adopted here to provide a cost-effective route to manipulate the valence state of Eu in Eu:  $\text{Al}_2\text{O}_3$ . Eu was introduced in the form of  $\text{Eu}_2\text{O}_3$  (99.5%, Sigma-Aldrich) and high-purity  $\alpha$ - $\text{Al}_2\text{O}_3$  powder (>99%) (CR-10, Baikowski, Annecy, France,  $D_{50} = 0.45 \mu\text{m}$ ) was used as the matrix material. After drying and de-binding of gelled Eu:  $\text{Al}_2\text{O}_3$ , the material is sintered in a vacuum furnace ( $10^{-3}$ - $10^{-4}$  Pa) at the temperature 1400-1850 °C for 8 hours with the final sample diameter around 3 mm and thickness in the range of 3-5 mm.

After sintering, the room temperature photoluminescence emission and excitation spectra of Eu:  $\text{Al}_2\text{O}_3$  were recorded in an apparatus consisting of a Xenon lamp, two grating monochromators and a synchronous light detection system (Fluorolog-Tau-3, Jobin Yvon Inc. Horiba, Japan). The measurements were performed with internal corrections and compensation for the light source. Decay curves were also recorded using a pulsed Nd:YAG laser at 266 nm or 355 nm (Spectron Laser System SL802G, Rugby, UK) with a pulse energy of approximately 5 mJ, 10 Hz repetition rate and 5 ns duration.

## 3. Results and discussion

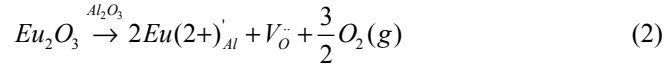
### 3.1 Density functional theory simulations with $U$ correction (DFT + $U$ ) of $\text{Eu}^{2+}/\text{Eu}^{3+}$ : $\alpha$ - $\text{Al}_2\text{O}_3$

We first investigated the defect mechanism for Eu doping in  $\alpha$ - $\text{Al}_2\text{O}_3$ . Mössbauer measurement has indicated that the  $\text{Eu}^{3+}$  dopant in  $\alpha$ - $\text{Al}_2\text{O}_3$  has a coordination number of six [28]. There have also been previous work hypothesizing that the  $\text{Eu}^{3+}$  dopant would substitute  $\text{Al}^{3+}$ , rather than occupy interstitial sites, based on the bonding covalency and similar X-ray diffraction pattern between pure and doped alumina [28, 29]. In this study, we examined both substitution and interstitial mechanisms. The preferred one was found to be the substitution of  $\text{Al}^{3+}$  by  $\text{Eu}^{3+}$  as described by the following defect reaction in Eq. (1):



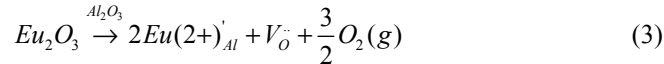
This should come as no surprise even though both  $\text{Al}^{3+}$  substitution and octahedral interstitial (tetrahedral interstitial site is too small for large ion such as  $\text{Eu}^{3+}$ ) provide the same coordination environment for  $\text{Eu}^{3+}$ . The interstitial mechanism places  $\text{Eu}^{3+}$  adjacent to  $\text{Al}^{3+}$  ions, causing strong lattice distortions. It also needs to be charge compensated by  $\text{O}^{2-}$  interstitials or  $\text{Al}^{3+}$  vacancies, incurring large energetic penalties.

Interestingly,  $\text{Eu}^{2+}$  dopant also prefers a similar substitution mechanism, even though both substitution and interstitial require other defects (considering the most likely mechanisms: one  $\text{O}^{2-}$  vacancy per two  $\text{Eu}^{2+}$  substitutions versus one  $\text{O}^{2-}$  interstitial per one  $\text{Eu}^{2+}$  interstitial). The defect reaction equation, describing the reduction of  $\text{Eu}^{3+}$  to  $\text{Eu}^{2+}$  in  $\text{Al}_2\text{O}_3$  host lattice, can therefore be written as Eq. (2):



It is worth noting that both isolated  $Eu^{3+}$  and  $Eu^{2+}$  substations have six-coordinated environments. For both cases, the first coordination shell is well-defined and similar to that of  $Al^{3+}$  in  $Al_2O_3$ , with two sets of Eu-O bond lengths. It can be seen that, in spite of the substantial size difference between europium and aluminum ions, isolated Eu dopant can be constricted by the host lattice and assume the environment of host cations, at least at a low dopant concentration. This can also apply to other host materials for selecting desired local environment for the luminescence dopant.

As both  $Eu^{3+}$  and  $Eu^{2+}$  would assume the same lattice site, the reduction reaction of  $Eu^{3+}$  to  $Eu^{2+}$  can be written as the following Eq. (3), by combining Eq. (1) and (2):



The reduction enthalpy for this reaction can then be calculated in Eq. (4):

$$E_r = E_{2Eu^{2+}} + E_{V_{O}^{\cdot\cdot}} + \mu_O(T, P) - E_{2Eu^{3+}} \quad (4)$$

where  $(E_{2Eu^{2+}} - E_{2Eu^{3+}})$  is the difference in lattice energy between  $Eu^{2+}$  and  $Eu^{3+}$  doped structures, and  $\mu_O(T, P)$  is calculated as:

$$\mu_O(T, P) = \frac{1}{2}E_{O_2} + \Delta\mu_O^0(T) + k_B T \ln(p_{O_2}) \quad (5)$$

where  $E_{O_2}$  is the energy of  $O_2$  molecule at 0K, which was calculated from DFT by placing an isolated  $O_2$  molecule in the simulation box. The standard chemical potential of oxygen at higher temperatures can be calculated by correcting  $E_{O_2}$  with  $\Delta\mu_O^0(T)$ , which is obtained from thermodynamic tables [30]. The DFT + U simulations calculated the value of  $(E_{2Eu^{2+}} + E_{V_{O}^{\cdot\cdot}} + \frac{1}{2}E_{O_2} - E_{2Eu^{3+}})$  as 3.50 eV. Using this value, the reduction level can be estimated as a function of oxygen partial pressure according to reaction kinetics theory. Ignoring the vibrational entropy contribution, the temperature-dependence equilibrium constant follows the Boltzmann distribution:

$$\frac{[Eu'_{Eu}]^2 [V_{O}^{\cdot\cdot}]}{[Eu^{\times}_{Eu}]^2 [O_O^{\times}]} = \exp\left(-\frac{E_r}{kT}\right) \quad (6)$$

where  $[Eu'_{Eu}]$ ,  $[Eu^{\times}_{Eu}]$ ,  $[V_{O}^{\cdot\cdot}]$ ,  $[O_O^{\times}]$  are equilibrium concentrations of  $Eu^{2+}$ ,  $Eu^{3+}$ , oxygen vacancies, and oxygen ions, respectively, and they satisfy:

$$[Eu'_{Eu}] = 2[V_{O}^{\cdot\cdot}] \quad (7)$$

and, considering that  $[V_{O}^{\cdot\cdot}] + [O_O^{\times}]$  gives the total concentration of oxygen sites in the host  $Al_2O_3$ :

$$\frac{[Eu'_{Eu}] + [Eu^{\times}_{Eu}]}{[V_{O}^{\cdot\cdot}] + [O_O^{\times}]} = \frac{[Eu'_{Eu}] + [Eu^{\times}_{Eu}]}{\frac{3}{2}[Al^{\times}_{Al}]} = \frac{2}{3}c_{Eu} \quad (8)$$

where  $c_{Eu}$  is the doping concentration of Eu. Solving Eqs. (6), (7) and (8), the  $Eu^{2+}$  concentration can be obtained. The results are plotted in Fig. 1. The  $Eu^{2+}$  concentration shows a dependence on oxygen partial pressure with a characteristic exponent of  $-1/6$ . At high

oxygen partial pressure, reduction is limited. Typical vacuum furnaces for high temperature sintering can maintain oxygen partial pressure in the range of  $0.21 \times (10^{-3}-10^{-4})$  Pa, which is marked with the dotted lines. It can be seen that, for  $p(O_2)$  in this range, a high temperature above 1700°C can reduce majority (>95%) of the  $\text{Eu}^{3+}$  to  $\text{Eu}^{2+}$ . Such a high temperature can also encourage oxygen diffusion so that the reduction equilibrium can be reached efficiently.

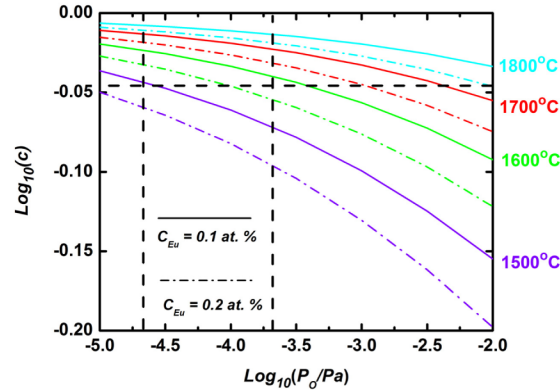


Fig. 1. Calculated  $\text{Eu}^{2+}$  concentration (in  $\log_{10}(c)$ , where  $c = [\text{Eu}^{2+}]/[\text{Eu}]$ ) versus oxygen partial pressure (in  $\log_{10}(P_O)$ , where  $P_O$  is oxygen partial pressure in Pa) in the temperature range between 1400~1900 °C. Vertical dashed lines mark the range of oxygen partial pressure used in vacuum synthesizes. The horizontal dashed line indicates  $c = 95\%$ .

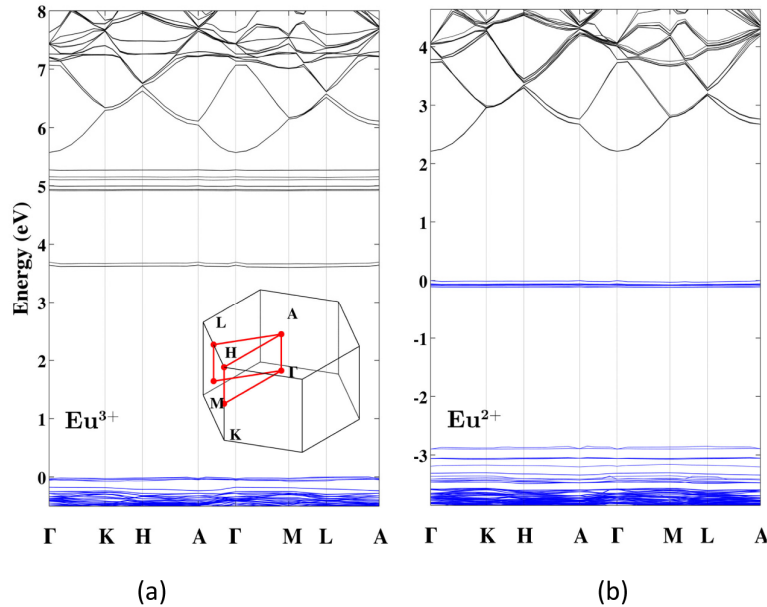


Fig. 2. Band structure of  $\text{Eu}^{3+}$  (a) and  $\text{Eu}^{2+}$  (b) doped alumina. The Fermi energy is set to 0 eV. For comparison, the two plots are arranged so that the energy levels contributed mainly by alumina are aligned. For clarity, unoccupied and occupied bands are shown in blue. Spin up and spin down levels are plotted with solid and dotted lines, respectively.

The electronic band structures of  $\text{Eu}^{3+}$  and  $\text{Eu}^{2+}$  doped  $\alpha\text{-Al}_2\text{O}_3$  are also calculated from the DFT + U simulations, as shown in Fig. 2. We observe no substantial differences between the electronic bands contributed by the host material,  $\alpha\text{-Al}_2\text{O}_3$  between the two cases. The defect states contributed by the dopants in the band gap are well defined, and show no obvious characteristics of the  $\alpha\text{-Al}_2\text{O}_3$  symmetry. Therefore, we expect the luminescence in

both cases to retain its characteristic spectrum. However, it is worth noting that the effect of oxygen vacancy, especially the association between the dopant and vacancy, is not considered here. This could potentially cause alterations of the spectrum of the  $\text{Eu}^{2+}$  doped material, which warrants further investigations.

### 3.2 Photoluminescence characterization of $\text{Eu}^{2+}/\text{Eu}^{3+}:\text{Al}_2\text{O}_3$

#### 3.2.1 Room temperature photoluminescence emission and excitation of $\text{Eu}^{2+}/\text{Eu}^{3+}:\text{Al}_2\text{O}_3$

Room temperature photoluminescence excitation and emission spectra of  $\text{Eu}:\text{Al}_2\text{O}_3$  were recorded in Fig. 3 and Fig. 4. The photoluminescence excitation spectrum of  $\text{Eu}^{2+}:\text{Al}_2\text{O}_3$  (Fig. 3) shows two over-lapped excitation peaks with the centers at 277 nm and 330 nm, coming from the emission behavior of  $\text{Eu}^{2+}$ . The blue emission of  $\text{Eu}:\text{Al}_2\text{O}_3$  comes from the transition of  $\text{Eu}^{2+}$  between  $4f^65d^1$  and  $4f^7$  ( $^8S_{7/2}$ ) ( $\text{Eu}^{2+}(4f^7) + h\nu \rightarrow \text{Eu}^{2+*}(4f^65d^1)$ ). Such f-d transition and broadband emission are usually strongly dependent on the local atomic environment of the activation center. Gaussian fitting analysis of the excitation spectrum of vacuum-sintered  $\text{Eu}^{2+}:\text{Al}_2\text{O}_3$  (monitored at 430 nm, Fig. 3) showed two broad excitation peaks at 277 nm and 330 nm, respectively, indicating that the  $\text{Eu}^{2+}$  ions are located in low-symmetry sites with a broad crystal field distribution [31] and a large field splitting of 5d band [29]. Such excitation spectrum is different from those measured for  $\text{Eu}^{2+}:\text{Al}_2\text{O}_3$  powder [29] and  $\text{Eu}^{2+}:\text{Al}_2\text{O}_3$  film [32]. It is possible that the fabrication process has led to changes in the local symmetry of the  $\text{Eu}^{2+}$  activator. As shown by the DFT + U calculations, the  $\text{Eu}^{2+}$  dopants substitute  $\text{Al}^{3+}$ , accompanied by oxygen vacancies. The oxygen vacancies may form  $\text{F}^+$ -centers [33], and contribute to broad excitation and emission spectra in the UV region. Additionally, strong association may exist between dopants and vacancies. Under favorable synthesis conditions, e.g. slow cooling rate, defect clusters such as  $\text{Eu}(2+)_{\text{Al}} - V_{\text{O}}^{\bullet\bullet}$  may be obtained, which leads to a change in the local symmetry of the  $\text{Eu}^{2+}$  activator and, consequently, the crystal field felt by  $\text{Eu}^{2+}$  ions. Indeed, the bulk samples may experience slower cooling in the center than powders and films even when the same nominal cooling rate is used [34]. Other factors, such as phase separation, defect segregation at grain boundary, etc., could also contribute to the changes in the local atomic environment of the activation centers, which warrants further investigations.

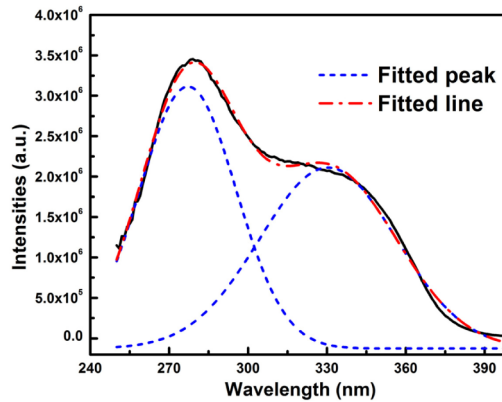


Fig. 3. Room temperature photoluminescence excitation spectra of vacuum-sintered 0.1at%  $\text{Eu}^{2+}:\text{Al}_2\text{O}_3$  monitored at 430 nm with corresponding Gaussian fitting curves.

Air-sintered  $\text{Eu}:\text{Al}_2\text{O}_3$  was also examined under excitation by UV light (277 nm), which showed the characteristic photoluminescence peaks of  $\text{Eu}^{3+}$  at 588 nm ( $^5\text{D}_0\text{-}^7\text{F}_1$ ) and 611 nm ( $^5\text{D}_0\text{-}^7\text{F}_2$ ) [35–37]. In comparison, under excitation with UV light (277 nm and 330 nm),

vacuum sintered  $\text{Eu}:\text{Al}_2\text{O}_3$  only showed one broad peak in the wavelength range of 330-600 nm with a peak center near 430 nm but none of the characteristic peaks of  $\text{Eu}^{3+}$ . This indicates that the reduction of  $\text{Eu}^{3+} \rightarrow \text{Eu}^{2+}$  in the  $\text{Al}_2\text{O}_3$  host was achieved by vacuum sintering at temperatures of 1750-1850 °C, as predicted by the DFT + U calculations.

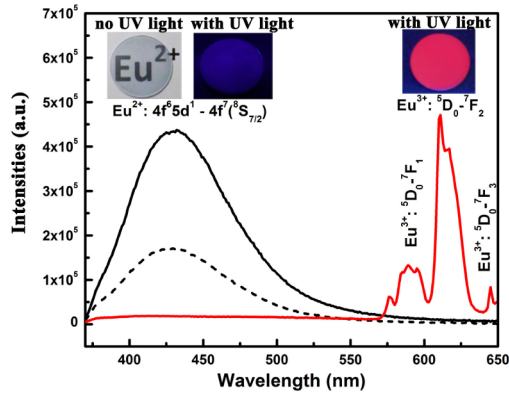


Fig. 4. Room temperature photoluminescence emission spectra of vacuum-sintered 0.1at%  $\text{Eu}^{2+}:\text{Al}_2\text{O}_3$  and air-sintered 0.1at%  $\text{Eu}^{3+}:\text{Al}_2\text{O}_3$  excited with 277 nm and 330 nm (dark line:  $\text{Eu}^{2+}:\text{Al}_2\text{O}_3$ ; red line:  $\text{Eu}^{3+}:\text{Al}_2\text{O}_3$ ).

### 3.2.2 Room temperature photoluminescence emission spectra of $\text{Eu}:\text{Al}_2\text{O}_3$ sintered at varying vacuum-sintering temperature

To further validate the DFT + U calculations, samples were vacuum sintered at different temperatures using the same procedure. The measured emission spectra were shown in Fig. 5. As expected, the intensity of the characteristic  $\text{Eu}^{3+}$  photoluminescence peak at 611 nm ( $^3\text{D}_0\text{-}^7\text{F}_2$ ) decreases with increasing vacuum sintering temperature. In comparison, the emission intensity of  $\text{Eu}^{2+}$  in the blue light region increases with higher vacuum sintering temperature. The presence of  $\text{Eu}^{3+}$  is evident at and below 1700 °C, suggesting the calculated  $\text{Eu}^{2+}$  concentration may be overestimated, which requires further quantification. Nonetheless, the DFT + U calculations provided adequate guidance for selecting the correct sintering condition. It should also be noted that, low porosity and good sintering quality in the samples, a prerequisite for optical applications that require high transmittance, have been obtained at temperatures above 1700 °C.

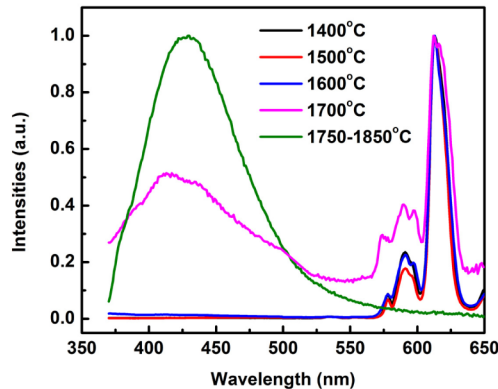


Fig. 5. Photoluminescence spectra of vacuum-sintered 0.1at%  $\text{Eu}^{2+}:\text{Al}_2\text{O}_3$  at room temperature excited with 277 nm as a function of vacuum sintering temperature (normalized to the same height at the spectra maxima).

### 3.2.3 Luminescence decay properties of $\text{Eu}^{2+}:\text{Al}_2\text{O}_3$

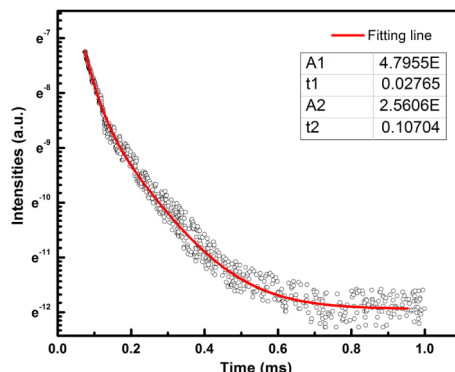


Fig. 6. Decay curve of 0.1at%  $\text{Eu}^{2+}:\text{Al}_2\text{O}_3$  (sintering temperature: 1750°C-1850°C) monitored at 490 nm with the excitation 266 nm at room temperature.

The luminescence decay curve of the vacuum sintered (1750°C-1850°C) 0.1 at. %  $\text{Eu}^{2+}:\text{Al}_2\text{O}_3$  measured at room temperature is shown in Fig. 6, monitored at 490 nm with an excitation wavelength of 266 nm. The luminescence decay curves were fitted by double exponentials ( $I = A_1 * \exp(-t_1/\tau_1) + A_2 * \exp(-t_2/\tau_2)$ ) with the equation parameter shown in Fig. 6. The decay time of the  $\text{Eu}^{2+}$  d-f transition is on the order of microseconds. The average decay time of the  $\text{Eu}^{2+}$  in  $\text{Al}_2\text{O}_3$  after vacuum-sintering was calculated from the fitting process to be approximately 0.080 ms.

## 4. Summary

Overall, it can be seen that ab-initio calculations employing an improved DFT + U method for rare earth elements successfully guided the fabrication of Eu in  $\alpha\text{-Al}_2\text{O}_3$  host. The simulation results showed that  $\text{Eu}^{2+}:\text{Al}_2\text{O}_3$  can be fabricated by gelcasting and a subsequent vacuum sintering process under a vacuum atmosphere of  $10^{-3}$ - $10^{-4}$  Pa in the temperature region of 1750°C-1850 °C. The resultant materials show strong photoluminescence behavior with an average lifetime of 0.080 ms. Additionally, the DFT + U calculations also provided details regarding the lattice distortions and defect associations. The presented method can be easily applied to other rare earth dopants and other host materials.

## Funding

Air Force Office of Scientific Research (AFOSR) (FA9550-14-1-0155).